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# 1 Introduction











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a

(a)

a

hnoh\_0 1 Tf ( )Tj /T3\_1 1 Tf 2.143 0 5ng)so



d a

$$V(d) = \max_{a; f; d^0} (1-f)s + f(1-a)(1 + V(d^0) - V(d)) + V^0(d)d$$

$$d \quad a \quad 7$$

$$a(d) \quad f(d)$$

$$W(d) = f(d) (a(d) + (1 - a(d))(W(d^0) - W(d)) + W^0(d)d$$

$$\max_{a \in [0;1]} a + (1 - a) (W(d^0) - W(d));$$

$$a$$

$$W(d^0) - W(d) \begin{cases} \geq 1 & a(d) = 0 \\ = 1 & a(d) = 1 \\ < 1 & 0 < a(d) < 1 \end{cases}$$

### 3.2 The Pareto Frontier

V



$V(d)$

$s$

$$\frac{d-x}{d}s + \frac{x}{d}V(d)$$

$$s = V(0)$$

$$d = 0$$

$s$

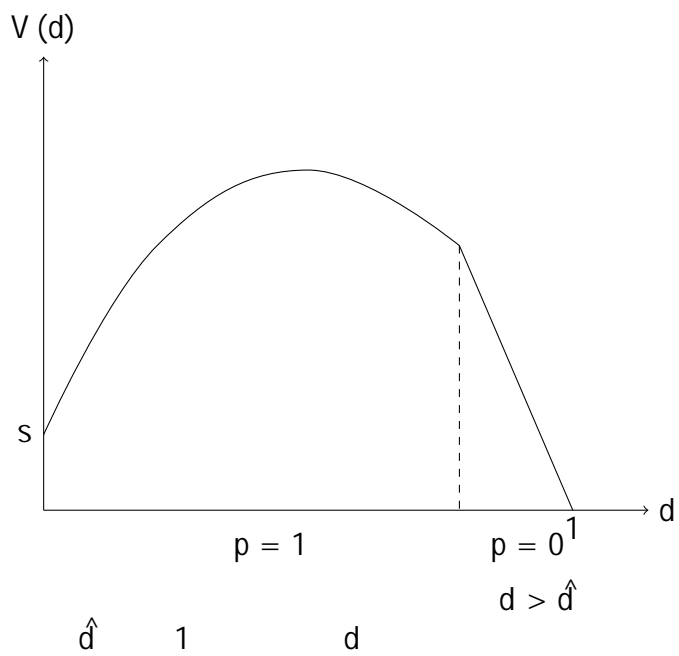
$V(x)$

$$V(x) = \frac{d-x}{d}V(0) + \frac{x}{d}V(d)$$

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$$a = 0$$





$d = 0$   
 $\hat{d}$   
 $e > 0$  T  
 $e;$  E  
 $f(d) > 0$   $d f$   $d$   $o(f_T)$   
 just

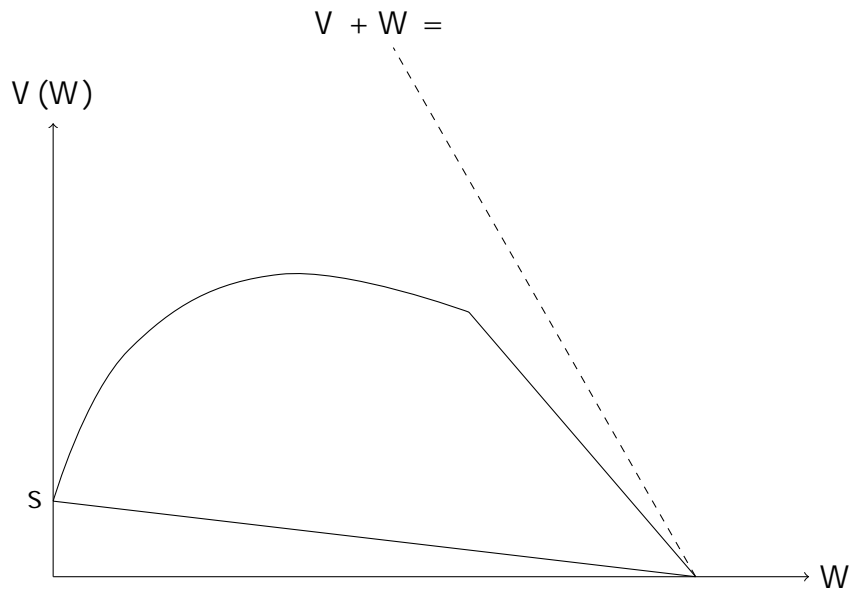
$$\begin{aligned}
 W &= f((1-a) + a) + W \\
 &= f + W
 \end{aligned}$$

$W(d)$

$V \quad W \quad d$

$W = W(d)$

d



C

C -

$a = 0$

C

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## 4 Disclosure and Competition Policy

### 4.1 Disclosure

$$ua_u \quad a_u \quad 1 - a_m \quad u$$

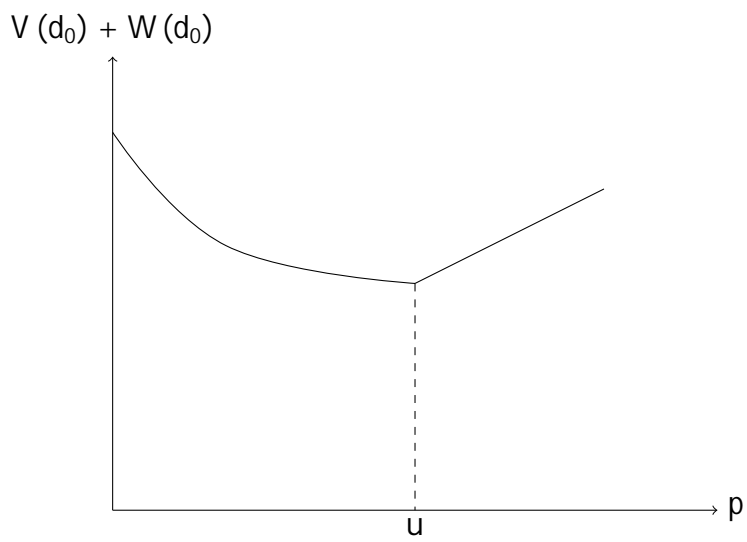
u

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a







#### 4.1.2 Alternative policies

$d$

$\hat{d}$

$d < \hat{d}$ ;

making

f<sup>14</sup>

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$$\underline{V}(d) + V^s = 1 \quad s = 0$$

**Lemma 6.**  $V(d) = \underline{V}(d) + s(1 - d)$

d

$$s \quad s \quad dV=ds \quad V$$

$$V(d) = \max_{a,f} (1 - f)s + f(1 - a) \left( (1 - s)(d^0 - d) + V^0(d)d \right)$$

$$a = 0 \quad f = 1$$

$$\begin{aligned} dV=ds &= - (d^0 - d) - d \\ &= - (d^0 - d) - (d - 1 - (d^0 - d)) \\ &= 1 - d \end{aligned}$$

$$dV=d = 2(d^0 - d) + \underline{V}^0(d)d$$

$$s = 0$$

$$V(\hat{d}) \quad \frac{dV}{d\hat{d}} > 0 \quad \frac{V(\hat{d})}{s} \quad d = 0$$

□

$$- d_0 = (1 - d_0)$$

s

$$d_0 + (1 - d_0)s$$

$$\frac{dx}{ds} =$$

$d_0$

□

## 5 Extension

### 5.1 Limited commitment for the follower

$$V^0 = s \quad 16 \quad s$$

$$d = 1$$

$$d$$

Lemma .

$$f = 1 \quad d \quad d < d \quad f = 1$$

$$d = d \quad d \quad V(d) = s \quad d < d \quad f = 0$$

$$\frac{d-d}{d}s + \frac{d}{d}V(d) = s$$

□

$$f = 1 \quad a = 1 \quad d \quad d \quad d \quad d \quad V(d) = s \quad d > d$$

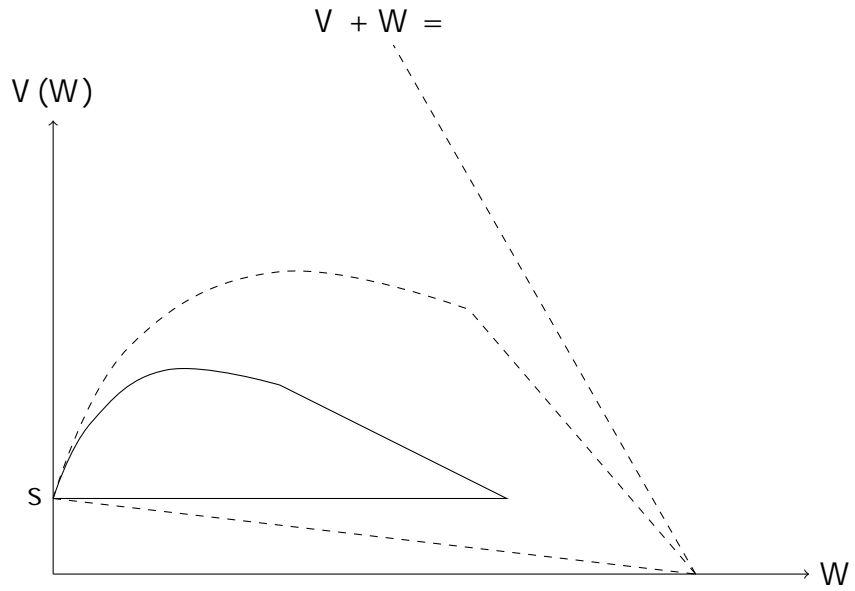
$$(d; 1]$$

$$d \quad d$$

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$d > \hat{d}$        $p(d) = 0$        $d < \hat{d}; p(d) = 1$        $d = 0$   
 $a(d) = 1$        $d = 0$        $V(0) = V(d) = s$        $V'(d) < 0$   
 $V$




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### 5.2.1 Known Transaction Value

$$a + v \quad v > 0$$

a

$$W(d) = f(d) (v + a(d) + (1 - a(d))p(d)(W(d^0) - W(d))) + W^0(d)d$$

$$W + V = d(v + s) + s$$

v

**Proposition 9.**  $dV(d) = dv > 0 \quad d \in (0; 1)$

$$v^0 > v$$

v

the simple interest rate  $i = \frac{v^0 - v}{v}$

□



$$a = 0 \qquad \tilde{f} = 1 \qquad a = 1$$

$$\qquad \qquad \qquad \tilde{=} = 0$$

v

### .3 Bad ad ice

s:

$$a \qquad \qquad \qquad + a \ b$$

$$\qquad -b$$

$$a = 1 \qquad \qquad \qquad \underline{d}$$

$$- (W(d^0) - W(d)) + \ b(W(\underline{d}) - W) \ 0$$

$$1 - (W(d^0) - W(d)) + \frac{b}{a}(W(\underline{d}) - W) \ 0$$

$$W(\underline{d}) < W$$

$$V(d) = \max_{a,f;d^0} (1-f)s + f(1-a) (1+V(d^0) - V(d)) + f a \ b(-b+V(\underline{d}) - V(d)) + V^0(d)d$$

$$V$$

$$a = 0 \qquad \qquad \qquad a = 1$$

$$V(\underline{d}) < V(d)$$

$$\qquad \qquad \qquad a$$

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j /T3\_0 1 Tf 1.944 0 Td33 0 Td (of)aTj /y)28f (Tj /T3\_1 1 Tf -28.354 -1.208 Td .)TGames. SanTheoryTj /T3\_1 1 Tf -28.354 -1.



# roofs

## Proof of Proposition 1

W

V

V

$$V^0(d)(d - 1) \quad a = 0 \quad a = 1 \quad a = 1 \quad V(d) =$$

$$\begin{aligned} V_{a=0}(d) - V_{a=1}(d) &= ((-s) - V^0(d))(d^0 - d) \\ &= W^0(d)(d^0 - d) > 0 \end{aligned}$$

$$\begin{aligned} \hat{d} \quad W \quad a < 1 \quad f(d) = 1 \quad a = 0 \\ a(d) < 1 \quad d^0) < \end{aligned}$$

## Proof of Lemma

Step 1: shape of  $W$  (and therefore  $V$ ) for any  $f$  and  $a$ .

- $a(d) = 1$   $f(d) = 0$   $W(d) = W^0(d)(d - 1)$   
 $V(d) = (1 - s)(d^0 - d) + V^0(d)(d - 1 - (d^0 - d))$
- $f(d) = 0$   $W(d) = W^0(d)d$   $V(d) = V^0(d)(d - 1 - (d^0 - d))$
- $f(d) = 1$   $a(d) = 0$   
 $V(d) = (1 - s)(d^0 - d) + V^0(d)(d - 1 - (d^0 - d))$   
 $d^0 - d = x$   $x^0 < 0$   $W^0 = (1 - s)x^0 + V^{00}(d - 1 - x) + V^0(1 - x^0)$   
 $x^0(V^0 - (1 - s)) = d = V^{00}$   
 $V^{00} = -x^0(1 - s - V^0) = d$   
 $= -x^0 W^0 = d$   
 $x^0 < 0$   $d > 0$   $W^0 > 0$   $V^{00} < 0$

Step 2: kink point where  $d^0 = 1$  378.267 Tf ( )Tj /T1\_1 1 Tf 1.903 0 Td (d)Tj

### Proof of Lemma 3

d

$$p = 0 \quad d$$

$$d - W = 1 \quad W = \frac{1}{1+d} \quad ( ) \quad W$$

$$\frac{d}{d} = \frac{1=(1+d)}{=(1+d)^2} = \frac{(1+d)}{=(1+d)^2} = \frac{1}{W}$$

$$\begin{aligned} V &= (1 + (1-d)s - V) + (s - V) \\ &= \frac{1 + (1-d)s + s}{1 + d} \\ &= \frac{1}{1+d} + \frac{(1+d)s}{1+d} - \frac{d s}{1+d} \\ \lim_{t \rightarrow \infty} V &= \frac{1}{1+W} + \frac{(1+W)s}{1+W} \\ &= \frac{W}{W+1} + s \end{aligned}$$

$$V > s$$

□